

This applies to the first edition of the text.

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# Time Series Analysis and Its Applications

## Errata2

(Second and Third Printings & Some Additional First Printing)

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### Chapter 1

- p8: Figure 1.5 caption: ... various locations ...
- p17: First equation on the page and first sentence of Example 1.13:  $Ew_t$  should be  $E(w_t)$  for consistent notation.
- p28: Table 1.2 p. 28: last column should be labeled  $n = 100$ .
- p62: Eqn (1.115):  $o_p(\delta_n)$  should be  $O_p(\delta_n)$ .
- p65: In statement of Theorem 1.3. Let  $x_i$ , for  $i = 1, \dots, n$  be ...
- p67: Above the expression for  $y_{mn}$ . For  $m > 2M$
- p67: Near bottom, replace  $m - (m - M - 1) = M + 1$  by  $m + 1 - (m - M) = M + 1$
- p68: Under (i).  $(n/r)^{(-1/2)} \rightarrow m^{1/2}$ :  $y_{mn} \xrightarrow{d} y_m$ .
- p68: Under (ii).  $\phi_m(\lambda)$
- p70: Under (i), modify second expression.

$$V_m = \sum_{h=-2m}^{2m} \gamma(h) = \sigma_w^2 \left( \sum_{j=-m}^m \psi_j \right)^2.$$

- p80: Problem 1.8: Should read: Let  $w_t$ , for  $t = 1, 2, \dots$

### Chapter 2

- p98: Eqn (2.21) + sign missing, should be  $\dots + \phi_p x_{t-p}$
- p109: In Example 2.11: should read “Because  $\gamma(1) = c\phi$ , ..., so the *specific* solution ...”
- p110: First paragraph of PACF section: should read “Hence, it is worthwhile ... that will behave like the ACF for *MA models*, but for AR models, ...”
- p117: First paragraph: Example 2.17 (*not* 2.16).
- p120: Section on Forecasting ARMA, change the third sentence to read: “Throughout, we assume  $x_t$  is a causal and invertible ARMA( $p, q$ ) process,  $\phi(B)x_t = \theta(B)w_t$ , where  $w_t \sim N(0, \sigma_w^2)$ .”
- p129: Above eqn (2.97): Add a space between the words **likelihood** and *becomes*.
- p151: First paragraph: “... to lag 30 ...” (*not* 36).
- p156: Eqn (2.136) should have  $\Theta_Q(B^s)$ .
- p156: Eqn (2.137): Remove parentheses from  $\Phi_P B^{Ps}$ .
- p161: Example 2.40: An ARIMA(1,1,0)  $\times$  (2,1,1)<sub>12</sub> fits better than the model suggested in the example, namely ARIMA(1,1,0)  $\times$  (0,1,1)<sub>12</sub>. It has a smaller AICc and the Q-statistic is no longer significant.
- p171: First line: ... per 10,000 (*not* 1,000).
- p175: Top paragraph (occurs twice): “... threshold of .04...” (not 0.4).
- p177: Line 5 from bottom. (2.158) instead of (2.159).
- p185: Above (2.177). The simplest ARCH model...
- p187: Equation (2.185), delete “ $\text{var}(y_t^2) =$ ” from the equation.
- p196: Below (2.203). Should read: ... (1.101) *to* (1.105) ... instead of *and*.
- p196: 2nd displayed equation after (2.203): Should read  $x_t = \psi(B)w_t = \dots$  [not  $x_t = \psi(B)z_t = \dots$ ].
- p203: Problem 2.11, first sum:  $a_i$
- p207: Problem 2.26, plus sign missing:  $\dots + \beta_q t^q \dots$

## Chapter 3

- p218: Below eqn(3.5), should read “...will be 72 months or ...”
- p272: In first line of first equation, write  $e^{2\pi i\nu u}$  instead of  $e^{2\pi i\nu h}$
- p272: Top equation, second integral:  $e^{2\pi i\nu u}$
- p272: Second line of equation:  $\gamma(u)$
- p273: In definition of  $I_n$ ,  $\exp(2\pi i t \nu_j)$  should be  $\exp(-2\pi i t \nu_j)$ .
- p287: Paragraph beginning Example 3.22. sine, not since; of the input; normal distribution.
- p289: Problem 3.1 (a): Remove extra ‘is’: “... and  $\phi$  is uniformly ...”
- p299: Problem 3.25. Add that  $v_t$  and  $w_t$  are normally distributed. Replace  $\text{var } w_t$  and  $\text{var } v_t$  by  $\text{var}(w_t)$  and  $\text{var}(v_t)$  for consistent notation.

## Chapter 4

- p301: Eqn (4.1): plus sign missing:  $\dots + \beta_{tq} z_{tq} + \dots$
- p302: Eqn (4.1) and below: Write  $w_{ti}$  instead of  $w_{it}$ , and write  $\text{cov}(w_{ti}, w_{tj})$  instead of  $\text{cov}(w_{it}, w_{jt})$  for consistency.
- p313: Last sentence: ... of Section T2.15 ... (not T2.16).
- p314: Line above eqn (4.43) should read: Thus, using the results of Theorems 2.2 (d) and 2.3 of Section T2.15, we can write ...
- p317: First and second equations on the page, the tranposes are transposed. They should be:

$$-2 \ln f(\mathbf{x}_{t-1}, \mathbf{x}_t | Y_n) \propto (\mathbf{x}_{t-1} - \mathbf{x}_{t-1}^{t-1})' [P_{t-1}^{t-1}]^{-1} (\mathbf{x}_{t-1} - \mathbf{x}_{t-1}^{t-1}) + (\mathbf{x}_t - \Phi \mathbf{x}_{t-1})' Q^{-1} (\mathbf{x}_t - \Phi \mathbf{x}_{t-1}) + d(\mathbf{x}_t),$$

$$l(\mathbf{x}_{t-1}) = (\mathbf{x}_{t-1} - \mathbf{x}_{t-1}^{t-1})' [P_{t-1}^{t-1}]^{-1} (\mathbf{x}_{t-1} - \mathbf{x}_{t-1}^{t-1}) + (\mathbf{x}_t^n - \Phi \mathbf{x}_{t-1})' Q^{-1} (\mathbf{x}_t^n - \Phi \mathbf{x}_{t-1}),$$

- p324: In (4.69),  $n \ln |Q|$  and  $n \ln |R|$ .
- p327: In (4.79).  $\Phi K \mathbf{y}_t$  instead of  $K \mathbf{y}_t$ ,  $\Phi K \boldsymbol{\epsilon}_t$  instead of  $K \boldsymbol{\epsilon}_t$ .
- p328: The second paragraph on controllability should be corrected as follows:

In a similar manner, to define **controllability**, write the state noise as  $\mathbf{w}_t = B \mathbf{u}_t$ , where  $B$  is  $p \times r$  and  $\mathbf{u}_t$  is an  $r$ -dimensional, nonsingular, white noise process. Thus, the state equation is  $\mathbf{x}_t = \Phi \mathbf{x}_{t-1} + B \mathbf{u}_t$ . If the matrix  $C = [B, \Phi B, \Phi^2 B, \dots, \Phi^{p-1} B]$  has full rank  $p$ , the process is said to be controllable (or **reachable**). Controllability has to do with the fact that the state equation, satisfies

$$\mathbf{x}_{t+p} = \sum_{j=0}^{p-1} \Phi^j B \mathbf{u}_{t+p-j} + \Phi^p \mathbf{x}_t = C \mathbf{U}_t + \Phi^p \mathbf{x}_t,$$

where  $\mathbf{U}_t = (\mathbf{u}'_{t+p}, \dots, \mathbf{u}'_{t+1})'$ . If we think of the variables  $\{\mathbf{u}_{t+p}, \dots, \mathbf{u}_{t+1}\}$  as “controlling” the state output  $\mathbf{x}_t$ , and we act as if we are free to choose the  $\mathbf{u}_t$  at will, the fact that  $C$  is full rank means any desired value of  $\mathbf{x}_{t+p}$  can be obtained from any initial state  $\mathbf{x}_t$  by control of  $\mathbf{U}_t$ . In particular, we can put  $\mathbf{U}_t = C'(CC')^{-1} \mathbf{x}_{t+p} - \Phi^p \mathbf{x}_t$ .

- pp313-314: References to Section T2.16 should be to T2.15.
- p314: Below (4.43). The evaluation of  $P_t^t$  is easily computed as the conditional covariance corresponding to (4.43), namely

$$P_t^t = \text{cov}(\mathbf{x}_t | Y_{t-1}, \boldsymbol{\epsilon}_t) = P_t^{t-1} - P_t^{t-1} A_t' \Sigma_t^{-1} A_t P_t^{t-1},$$

which simplifies to (4.38).

- p338: Paragraph after P4.6: change *nonsingularity* to *singularity*.
- p338: After eqn (4.112): ...  $\text{cov}(w_t, v_t) = (\theta + \phi) \text{var}(v_t) = (\theta + \phi) R$ , ... [no square on the  $(\theta + \phi)$  term].
- p390: 8th line from top: “evidence of of some ...” remove extra of.
- p404: Problem 4.1 (c):  $\sigma_0^2$  instead of  $\sigma_0$  for consistency.
- p406: Problem 4.8 should begin: Let  $y_t$  represent the land-based global temperature series shown in Figure 4.2. The data file for this problem is HL.dat on the web site.

- p406: Problem 4.8(b): Change  $\nabla^3 x_t = w_t$  to  $\nabla^2 x_t = w_t$ , and change the hint to read: The state will be a  $2 \times 1$  vector, say  $\mathbf{x}_t = (x_t, x_{t-1})'$ .
- p407: Problem 4.10(b):  $P^2 - \phi^2 P - 1 = 0$
- p410: Problem 4.24 should have two parts. Fit . . . to: (a) the GNP residuals analyzed in Example 2.46 and compare the results to those obtained in that example; (b) the stock dividend yield series and compare the results to those obtained in Problem 2.43.

## Chapter 5

- p422: In (5.26).  $\beta_t^{M'}$
- p428: 3rd line below (5.40).  $\delta_t = 1$ .
- p436: In (5.68).  $h_r$  instead of  $h_t$ .
- p443: Near bottom:  $(\mu_t, \alpha_{1t}, \alpha_{2t}, \beta_{1t}, \gamma_{11t}, \gamma_{21t})'$
- p453: In (5.108).  $\Pi_j$  instead of  $\Pi_j(\mathbf{x})$ .
- p457: In  $g_2(\mathbf{x})$  near bottom.  $42.61x_1$ .
- p488: Above eqn (5.187):

$$f_x(\nu; \boldsymbol{\beta}) = \boldsymbol{\beta}' f_y(\nu) \boldsymbol{\beta} = \boldsymbol{\beta}' f_y^{\text{re}}(\nu) \boldsymbol{\beta}.$$

- p523: Problem 5.7:

$$\hat{A}(\nu) = \frac{B_w(\nu) - \phi(\nu)Y(\nu)}{1 - |\phi(\nu)|^2}$$